Q1.

3   The ninth term of an arithmetic progression is 22 and the sum of the first 4 terms is 49.

   (i) Find the first term of the progression and the common difference.   [4]

   The nth term of the progression is 46.

   (ii) Find the value of n.   [2]

Q2.

1   The first term of a geometric progression is 12 and the second term is –6. Find

   (i) the tenth term of the progression,   [3]

   (ii) the sum to infinity.   [2]

Q3.

8   A television quiz show takes place every day. On day 1 the prize money is $1000. If this is not won the prize money is increased for day 2. The prize money is increased in a similar way every day until it is won. The television company considered the following two different models for increasing the prize money.

   Model 1:   Increase the prize money by $1000 each day.

   Model 2:   Increase the prize money by 10% each day.

On each day that the prize money is not won the television company makes a donation to charity. The amount donated is 5% of the value of the prize on that day. After 40 days the prize money has still not been won. Calculate the total amount donated to charity

   (i) if Model 1 is used,   [4]

   (ii) if Model 2 is used.   [3]

Q4.

6   (a) A geometric progression has a third term of 20 and a sum to infinity which is three times the first term. Find the first term.   [4]

   (b) An arithmetic progression is such that the eighth term is three times the third term. Show that the sum of the first eight terms is four times the sum of the first four terms.   [4]

Q5.

7　(a)　The first two terms of an arithmetic progression are 1 and $\cos^2 x$ respectively. Show that the sum of the first ten terms can be expressed in the form $a - b\sin^2 x$, where a and b are constants to be found.　[3]

　　(b)　The first two terms of a geometric progression are 1 and $\frac{1}{3}\tan^2\theta$ respectively, where $0 < \theta < \frac{1}{2}\pi$.

　　　　(i)　Find the set of values of θ for which the progression is convergent.　[2]

　　　　(ii)　Find the exact value of the sum to infinity when $\theta = \frac{1}{6}\pi$.　[2]

Q6.

6　The first term of an arithmetic progression is 12 and the sum of the first 9 terms is 135.

　　(i)　Find the common difference of the progression.　[2]

The first term, the ninth term and the nth term of this arithmetic progression are the first term, the second term and the third term respectively of a geometric progression.

　　(ii)　Find the common ratio of the geometric progression and the value of n.　[5]

Q7.

4　The third term of a geometric progression is -108 and the sixth term is 32. Find

　　(i)　the common ratio,　[3]

　　(ii)　the first term,　[1]

　　(iii)　the sum to infinity.　[2]

Q8.

9　(a)　In an arithmetic progression, the sum, S_n, of the first n terms is given by $S_n = 2n^2 + 8n$. Find the first term and the common difference of the progression.　[3]

　　(b)　The first 2 terms of a geometric progression are 64 and 48 respectively. The first 3 terms of the geometric progression are also the 1st term, the 9th term and the nth term respectively of an arithmetic progression. Find the value of n.　[5]

Q9.

8　The first term of an arithmetic progression is 8 and the common difference is d, where $d \neq 0$. The first term, the fifth term and the eighth term of this arithmetic progression are the first term, the second term and the third term, respectively, of a geometric progression whose common ratio is r.

　　(i)　Write down two equations connecting d and r. Hence show that $r = \frac{3}{4}$ and find the value of d.　[6]

　　(ii)　Find the sum to infinity of the geometric progression.　[2]

　　(iii)　Find the sum of the first 8 terms of the arithmetic progression.　[2]

Q10.

6 **(a)** The fifth term of an arithmetic progression is 18 and the sum of the first 5 terms is 75. Find the first term and the common difference. [4]

(b) The first term of a geometric progression is 16 and the fourth term is $\frac{27}{4}$. Find the sum to infinity of the progression. [3]

Q11.

9 **(a)** A geometric progression has first term 100 and sum to infinity 2000. Find the second term. [3]

(b) An arithmetic progression has third term 90 and fifth term 80.

  (i) Find the first term and the common difference. [2]

  (ii) Find the value of m given that the sum of the first m terms is equal to the sum of the first $(m + 1)$ terms. [2]

  (iii) Find the value of n given that the sum of the first n terms is zero. [2]

Q12.

6 **(a)** The sixth term of an arithmetic progression is 23 and the sum of the first ten terms is 200. Find the seventh term. [4]

(b) A geometric progression has first term 1 and common ratio r. A second geometric progression has first term 4 and common ratio $\frac{1}{4}r$. The two progressions have the same sum to infinity, S. Find the values of r and S. [3]

Q13.

2 The first and second terms of a progression are 4 and 8 respectively. Find the sum of the first 10 terms given that the progression is

  (i) an arithmetic progression, [2]

  (ii) a geometric progression. [2]

Q14.

1 The first term of an arithmetic progression is 61 and the second term is 57. The sum of the first n terms is n. Find the value of the positive integer n. [4]

Q15.

5 The first term of a geometric progression is $5\frac{1}{3}$ and the fourth term is $2\frac{1}{4}$. Find

    (i) the common ratio, [3]

    (ii) the sum to infinity. [2]

Q16.

9 **(a)** In an arithmetic progression the sum of the first ten terms is 400 and the sum of the next ten terms is 1000. Find the common difference and the first term. [5]

    (b) A geometric progression has first term a, common ratio r and sum to infinity 6. A second geometric progression has first term $2a$, common ratio r^2 and sum to infinity 7. Find the values of a and r. [5]

Q17.

5 **(a)** In a geometric progression, the sum to infinity is equal to eight times the first term. Find the common ratio. [2]

    (b) In an arithmetic progression, the fifth term is 197 and the sum of the first ten terms is 2040. Find the common difference. [4]

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